

Show that:

$$\sum_{k=1}^n \binom{n}{k} \frac{(-1)^{k-1}}{1+s/k} = \prod_{k=1}^n \frac{1}{1+s/k}.$$

for  $\Re(s) \geq 1$ .